

ESOP - Recursion / Interface / Math

Assoc. Prof. Dr. Mathias Lux
ITEC / AAU

Let's recall ...



Base Data Types

Signed, two-complement integers

- long - 64 bit
- int - 32 bit
- short - 16 bit
- byte - 8 bit

Floating point numbers

- float - 32 bit
- double - 64 bit

Others

- char - 16-bit Unicode character
- boolean - true / false

Reference Data Types

Everything with „new“

- Arrays
- Objects

Wrapper Classes



- Byte, Short, Integer, Long, Float, Double
 - wrap base data types
- Wrapper classes are reference data types
 - no base data types!
- Wrapping is partially automated
 - Autoboxing & Unboxing
- Cp. class Boolean

Recursion



- A method $m()$ is called *recursive*, if it calls itself.
 - $m() \rightarrow m() \rightarrow m()$ directly recursive
 - $m() \rightarrow n() \rightarrow m()$ indirectly recursive

Recursion: Factorial n!



- Definition factorial
 - $n! = (n-1)! * n$
 - $1! = 1$
- Example
 - $4! = 4*3! = 4*3*2! = 4*3*2*1! = 4*3*2*1$

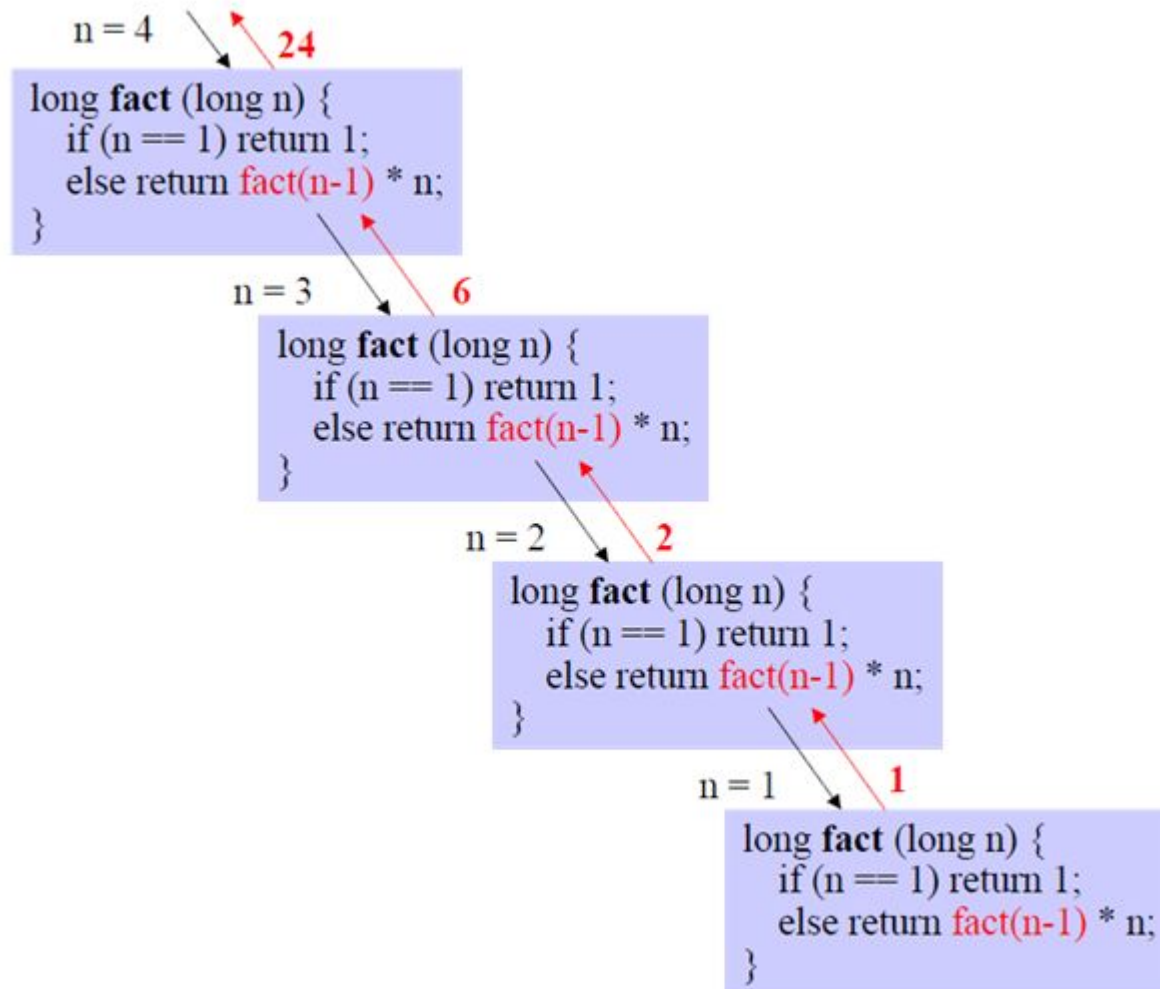
Recursion: Factorial n!



```
long fact (long n) {  
    if (n == 1)  
        return 1;  
    else  
        return fact(n-1) * n;  
}
```

End of recursion
when reaching 1!

Recursive Process



of `fact(...)`
and stores it

Example: Recursive Binary Search



Array has to be sorted!

	0	1	2	3	4	5	6	7
a	2	3	5	7	11	13	17	19
	↑			↑			↑	
	low			m			high	

	0	1	2	3	4	5	6	7
a	2	3	5	7	11	13	17	19
					↑	↑		↑
					low	m		high

- Find index m of the element in the middle
- $17 > a[m]$ -> search in right side of the array

```
static int search (int elem, int[] a, int low, int high) {  
    if (low > high) return -1; // empty  
    int m = (low + high) / 2;  
    if (elem == a[m]) return m;  
    if (elem < a[m]) return search(elem, a, low, m-1);  
    return search(elem, a, m+1, high);  
}
```

} non-recursive part

} recursion

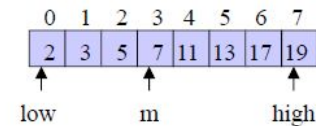
Example: Recursive Binary Search



elem = 17, low = 0, high = 7 ↑ 6

```
static int search (int elem, int[] a, int low, int high) {  
    if (low > high) return -1;  
    int m = (low + high) / 2;  
    if (elem == a[m]) return m;  
    if (elem < a[m]) return search(elem, a, low, m-1);  
    return search(elem, a, m+1, high);  
}
```

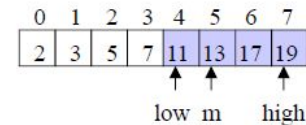
m = 3



low = 4, high = 7 ↓ ↑ 6

```
static int search (int elem, int[] a, int low, int high) {  
    if (low > high) return -1;  
    int m = (low + high) / 2;  
    if (elem == a[m]) return m;  
    if (elem < a[m]) return search(elem, a, low, m-1);  
    return search(elem, a, m+1, high);  
}
```

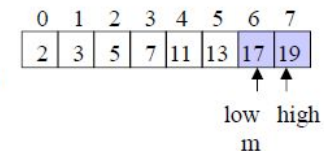
m = 5



low = 6, high = 7 ↓ ↑ 6

```
static int search (int elem, int[] a, int low, int high) {  
    if (low > high) return -1;  
    int m = (low + high) / 2;  
    if (elem == a[m]) return m;  
    if (elem < a[m]) return search(elem, a, low, m-1);  
    return search(elem, a, m+1, high);  
}
```

m = 6

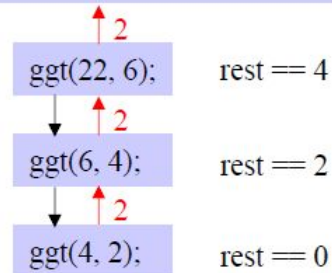


Example: GCD



recursive

```
static int ggt (int x, int y) {  
    int rest = x % y;  
    if (rest == 0) return y;  
    else return ggt(y, rest);  
}
```



iterative

```
static int ggt (int x, int y) {  
    int rest = x % y;  
    while (rest != 0){  
        x = y; y = rest;  
        rest = x % y;  
    }  
    return y;  
}
```

- Recursive algorithms can be implemented in an iterative way
 - recursive: often smaller program
 - iterative: often faster
- Recursion is extremely useful with some data structures (trees, graphs)

Example: Fibonacci Numbers



- $F_n = F_{n-1} + F_{n-2}$

```
public static int get(int number) {  
    if (number <= 2)  
        return 1;  
    return get(number-1) + get(number-2);  
}
```

Interfaces



- Class-like mechanism
 - for the definition of behaviour only.
- Allows for separation between definition and implementation
 - abstract data type

Interfaces



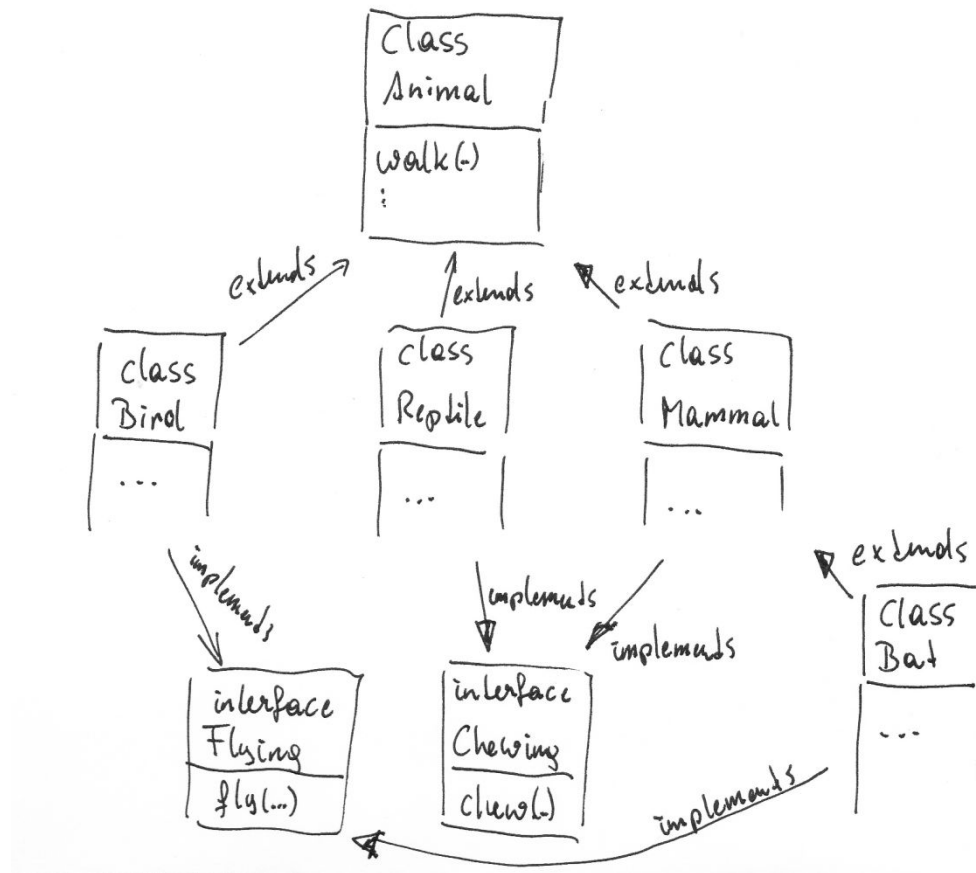
- Specification via `interface` keyword
- Method specifications
 - describe how to handle the implementing object.
 - without method body, just the head
- No object variables
 - Aber evt. Konstante

Interfaces



- The name of the interface can be used as a data type in Java.
- Implementation of an interface via `class`
 - implementing methods
 - having instance variables

Interface Example I



Interface Example II



[Overview](#) [Package](#) **[Class](#)** [Use](#) [Tree](#) [Deprecated](#) [Index](#) [Help](#)

Java™ 2 Platform
Standard Ed. 5.0

[PREV CLASS](#) [NEXT CLASS](#)

SUMMARY: [NESTED](#) | [FIELD](#) | [CONSTR](#) | [METHOD](#)

[FRAMES](#) [NO FRAMES](#) [All Classes](#)

DETAIL: [FIELD](#) | [CONSTR](#) | [METHOD](#)

java.lang

Interface Iterable<T>

All Known Subinterfaces:

[BeanContext](#), [BeanContextServices](#), [BlockingQueue](#)<E>, [Collection](#)<E>, [List](#)<E>, [Queue](#)<E>, [Set](#)<E>, [SortedSet](#)<E>

All Known Implementing Classes:

[AbstractCollection](#), [AbstractList](#), [AbstractQueue](#), [AbstractSequentialList](#), [AbstractSet](#), [ArrayBlockingQueue](#), [ArrayList](#), [AttributeList](#), [BeanContextServicesSupport](#), [BeanContextSupport](#), [ConcurrentLinkedQueue](#), [CopyOnWriteArrayList](#), [CopyOnWriteArraySet](#), [DelayQueue](#), [EnumSet](#), [HashSet](#), [JobStateReasons](#), [LinkedBlockingQueue](#), [LinkedHashSet](#), [LinkedList](#), [PriorityBlockingQueue](#), [PriorityQueue](#), [RoleList](#), [RoleUnresolvedList](#), [Stack](#), [SynchronousQueue](#), [TreeSet](#), [Vector](#)

```
public interface Iterable<T>
```

Implementing this interface allows an object to be the target of the "foreach" statement.

Method Summary

Iterator <I>	iterator() Returns an iterator over a set of elements of type T.
------------------------------	---

Method Detail

iterator

[Iterator](#)<I> [iterator\(\)](#)

Returns an iterator over a set of elements of type T.

When to use Interfaces?



- Making minimal functionality of an abstract data type visible
- Multiple inheritance
 - Graph, nicht Baum

Interface Examples



- Java Interfaces Iterable, Comparable und Serializable

NameGenerator



- How can a name generator be programmed with interfaces & inheritance?